

**AN INVESTIGATION INTO THE GROWTH
OF A BOILING BOUNDARY LAYER
IN TURBULENT FLOW**

John Calvin Dyer

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by

John Calvin Dyer

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OF A BOILING BOUNDARY LAYER IN
TURBULENT FLOW

by

Lieutenant John Calvin Dyer, U.S.N.

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ABSTRACT

The thickness of the boiling, bubble, boundary layer in forced convection flow in rectangular geometry was measured by photographs. The test section had a rectangular cross section (1/2 inch x 1/4 inch) which consisted of two opposite, electrically heated, stainless steel walls and two glass walls. The ratio of heated strip length to the spacing between the strips was about sixty. The range of the variables investigated was: heat flux density 0 to 475,000 Btu/hr ft²; test section flow velocity 0 to 5 ft/sec; pressure 0 to 56 psia, and liquid subcooling between 27°F and 108°F at the test section inlet.

The bubble boundary layer thickness was plotted against a parameter which expressed the calculated bulk subcooling of the liquid at the point where the bubble layer thickness was measured. The plots show quantitatively the behavior of the bubble layer under various conditions of subcooling, flow, and heat flux density. An attempt was made to include the conditions of nucleation of boiling as a unifying parameter for the layer growth. While a significant relationship was indicated, there is little experimental basis for the proper value of nucleation superheat necessary at the pressures investigated. In addition there are undoubtedly other nucleation variables which are significant. A generalized correlation of bubble layer growth was not achieved.

Thesis Supervisor: John A. Clark

Title: Assistant Professor of Mechanical Engineering

$$+2(5) = 6\% \quad +3(5) = 15\% \quad +4(5) = 20\% \Rightarrow$$

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He wishes to thank the craftsmen, particularly Robert Simpson, Herbert Norquist and William Liddy of the Central Tool Shop of the Boston Naval Shipyard for manufacturing the test section. Much credit is also given to Fred Johnson and Edward Hartell of the Heat Transfer Laboratory at the Massachusetts Institute of Technology for their ready assistance in the myriad details of assembling the test loop. In addition, the success of the photographic work was due to the skill and patience of Fred Johnson.

He also wishes to thank his wife, Glenys Dyer, who typed this thesis.

APPENDIX

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INTRODUCTION

The use of flat plate type fuel elements in nuclear reactors and the desire to achieve the higher heat transfer rates that are possible with the boiling process require more fundamental information on boiling under conditions of flat plate geometry. It was the objective of this investigation to make a photographic study of the boiling boundary layer growth under flow conditions using geometry and a ratio of coolant volume to heating surfaces which would more nearly approximate conditions in a nuclear reactor core. Previous investigations of pool boiling have generally used single heated wires or rods in a pool of water where the bubble size was large in relation to the heating surfaces, and the volume of fluid was much greater than the heating surface. The forced convection boiling has been done predominantly inside circular channels which is not the geometry of interest here.

Apparently the first work with rectangular flow channels was done by Gunther (1)* who had the heating strip in the center of the channel with water on both sides. As the intention was a study of bubble dynamics, rather than the growth of a bubble layer, the heated strips used by Gunther were not long. Argonne National

* Numbers in parentheses refer to the references in the bibliography.

Laboratory has done extensive work with flat plate geometry in boiling conditions, but the only published information to date has been for natural convection (2). The writer was informed that work on boiling in forced convection in rectangular flow channels had been done at AAI, but no reports were available.

None of the foregoing published investigations used forced convection in flow geometry with oppositely facing heating elements having a large L/y , ratio of length to spacing between plates. The heat transfer section which was used consisted of two electrically heated flat, stainless steel (18-8) strips with degassed (de-aerated) distilled water flowing between them. L/y for this experiment was about 60. The range of the variables investigated was: heat flux density 0 to 475,000 Btu/hr ft²; test section flow velocity 0 to 5 ft/sec; pressure at test section outlet 0 to 56 psia, and liquid subcooling between 27°F and 108°F at the test section inlet.

A description of the apparatus used, a discussion of the test procedure, and the test results are given in subsequent sections.

DESCRIPTION OF APPARATUS

The experimental equipment used to carry out this investigation is shown in the accompanying diagrams.

Fig. 1 is a schematic flow diagram of the test loop.

Fig. 2 is a photograph of the apparatus showing the test section in the vertical position. The pump and electrical preheaters are not visible in the photograph.

Distilled and degassed water was circulated in the test loop. This water was preheated before entering the test section by two electric heaters (electric Chromelox immersion heaters, type #1 270, 7000 watts, 240 volts, E.I. Wiegand Co., Pittsburh, Pa.). These heaters were controlled by Variacs, type V1002, General Radio Co., Cambridge, Mass. A simple coiled tube heat exchanger using cold water was used to cool the water leaving the test section before entering the pump (Westinghouse totally enclosed centrifugal pump, model 300, 220 volts, 3 phase, 60 cycles). This pump required an oil cooling system which had an oil to water section heat exchanger (Ross Heater and Manufacturing Co., Buffalo, N.Y.) and an electrically driven centrifugal pump, 10 hp, Allis Chalmers Manufacturing Co., Racine, Wis. The motor for the oil pump was 3/4 hp, 440 volt, 60 cycle, 3 phase, General Electric. The water circulating pump discharged to a 3/4 inch square edged orifice for flow

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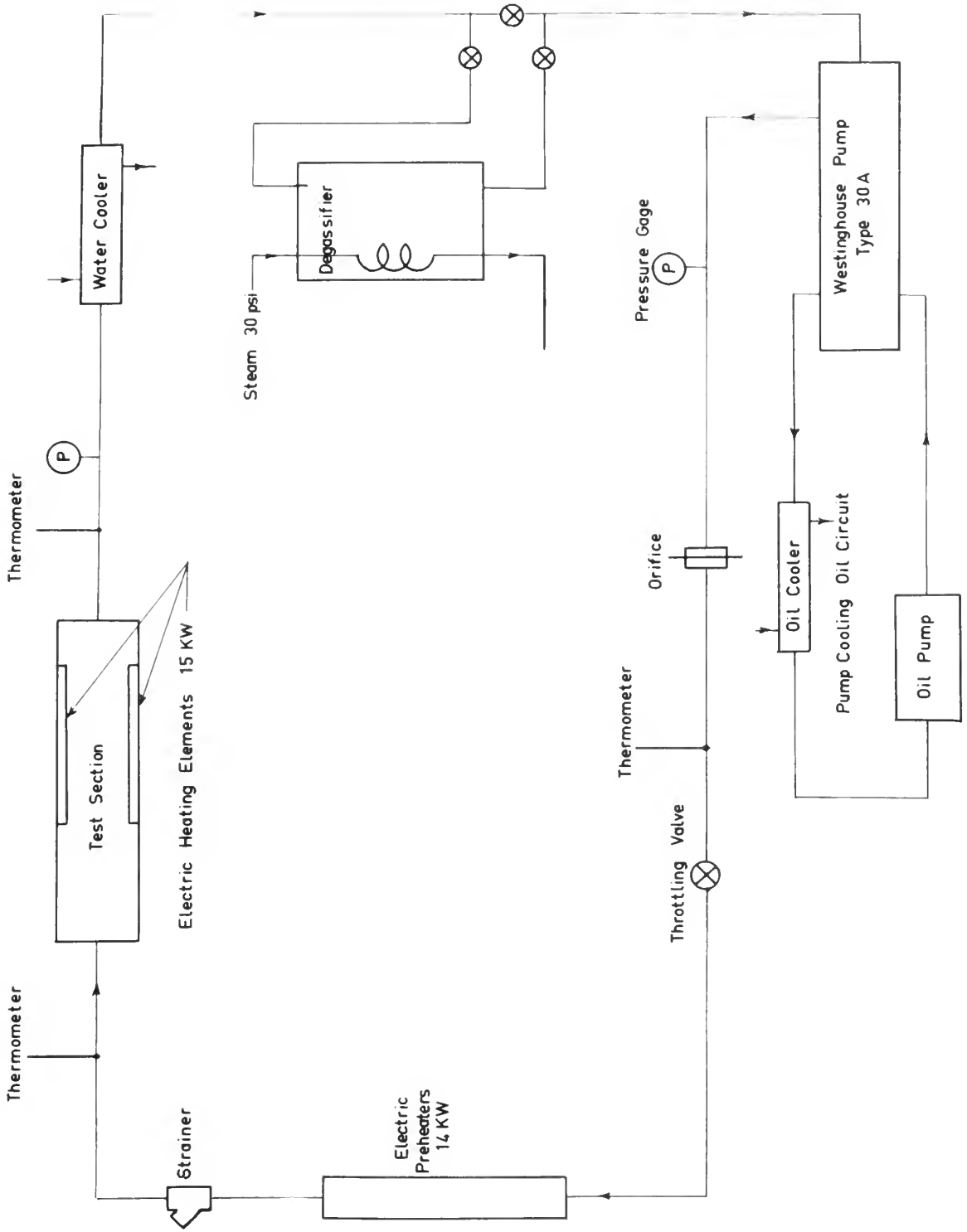


Fig. 1 - SCHEMATIC FLOW DIAGRAM

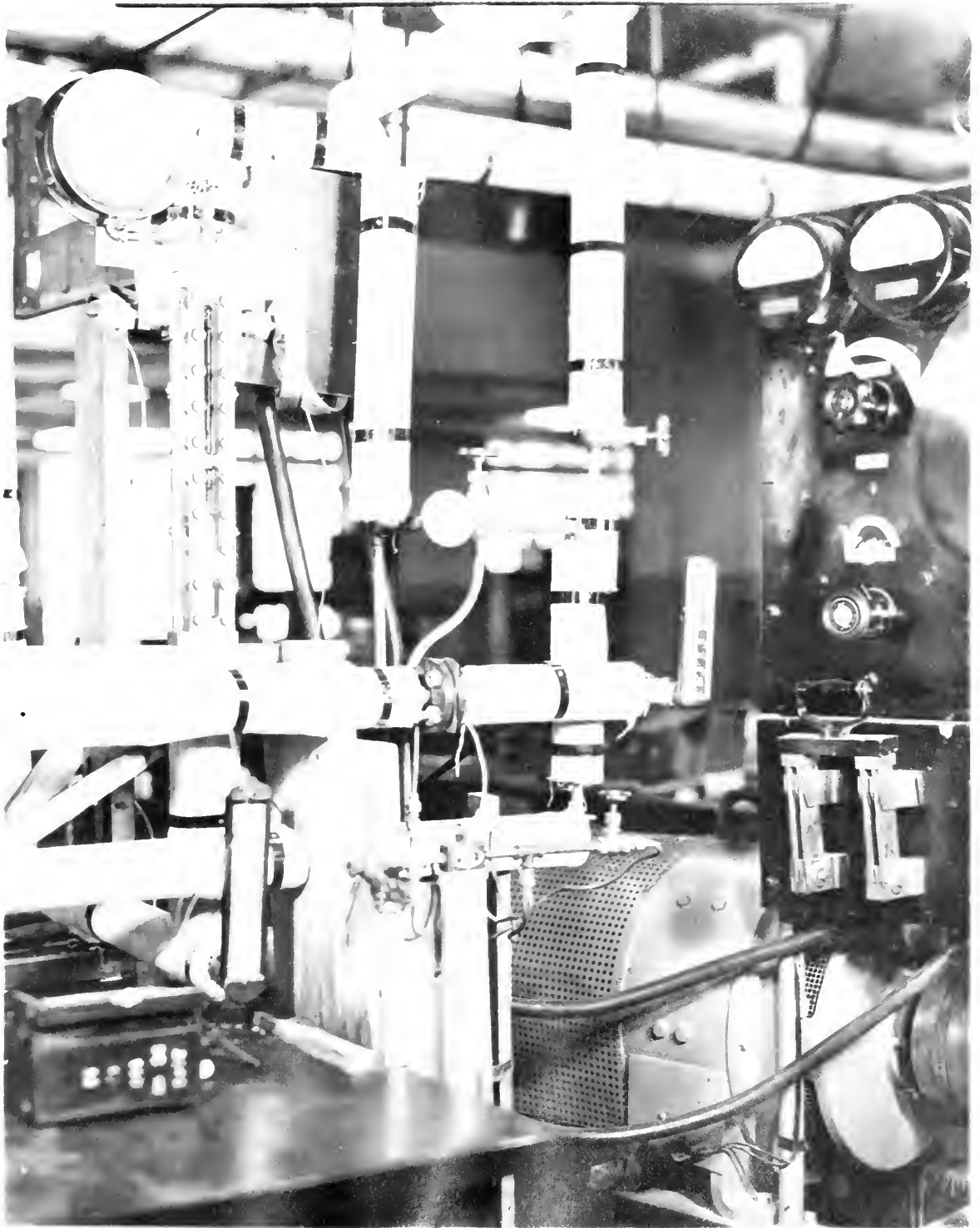


Fig. 2 - Photograph of Apparatus

measurements. The manometer used was a Merriam 20 inch U-manometer, type B-1103. The flow rate was controlled by a valve on the discharge side of the pump.

The test section consisted essentially of a rectangular flow channel, $1/4$ inch x $1/2$ inch cross section, with electrically heated stainless steel (18-8) strips forming two of the opposite walls. The other two walls were glass which permitted viewing the nucleate boiling bubble formation on the heated strips. The heated strips were 15.0 inches in length, giving an L/y of approximately 60. The inlet approach section was also rectangular, $1/4$ inch x $3/8$ inch cross section and an L/y of 50. The inlet and outlet sections (Fig. 3) were necessarily narrower, i.e. $3/8$ inch instead of $1/2$ inch to provide end support for the glasses. Tapered transitions were made at these points. The test section outlet had the same cross sectional dimensions as the inlet but was much shorter, about $3\ 1/2$ inches.

The main part of the test section was mild steel (Fig. 4). This provided a frame to receive the water inlet and outlet sections, the electrical conductors and heating strips, and the glass windows (Jerguson gage glasses, series 5, 17 inch length) which were clamped by modified Jerguson gage glass covers, series 5. Electrical insulation between the stainless steel heating strips and the mild steel frame was achieved by using

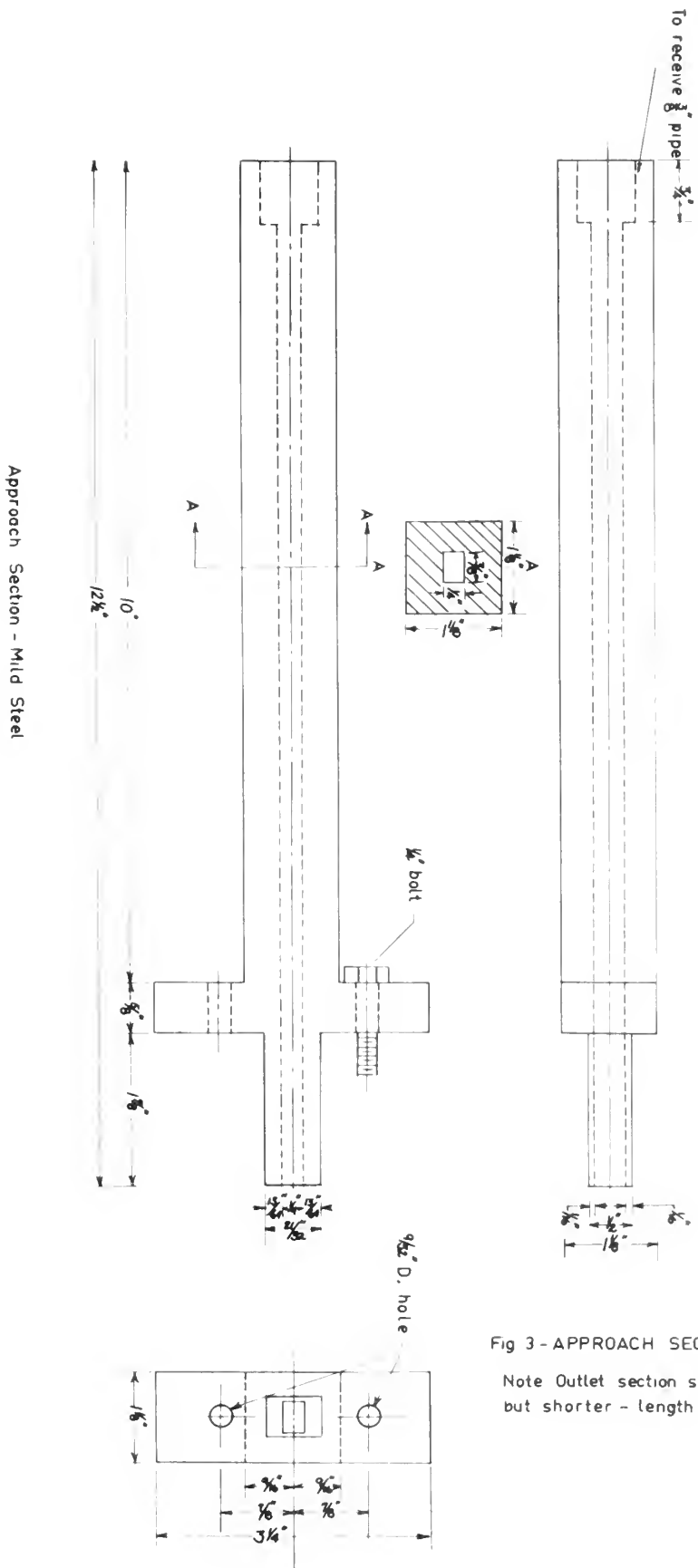


Fig 3 - APPROACH SECTION

Note Outlet section similar, but shorter - length $3\frac{1}{2}"$

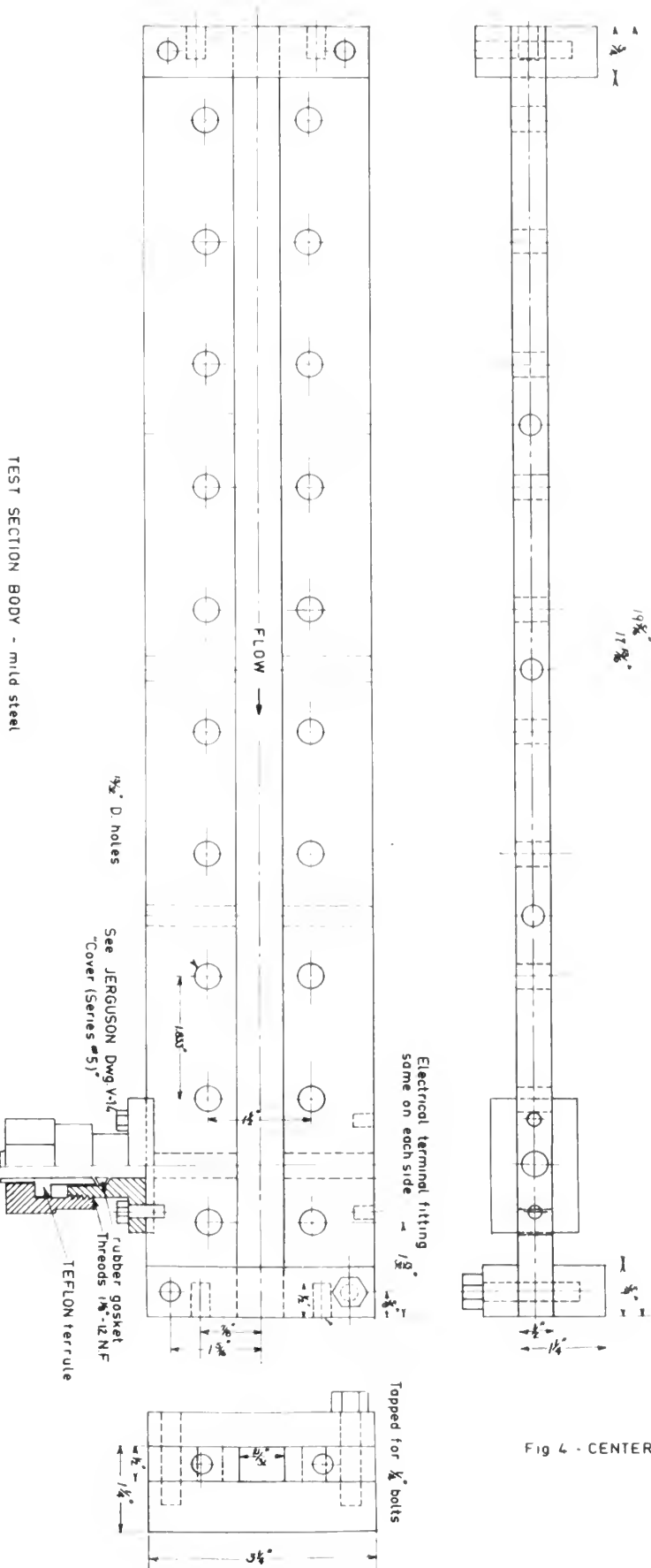


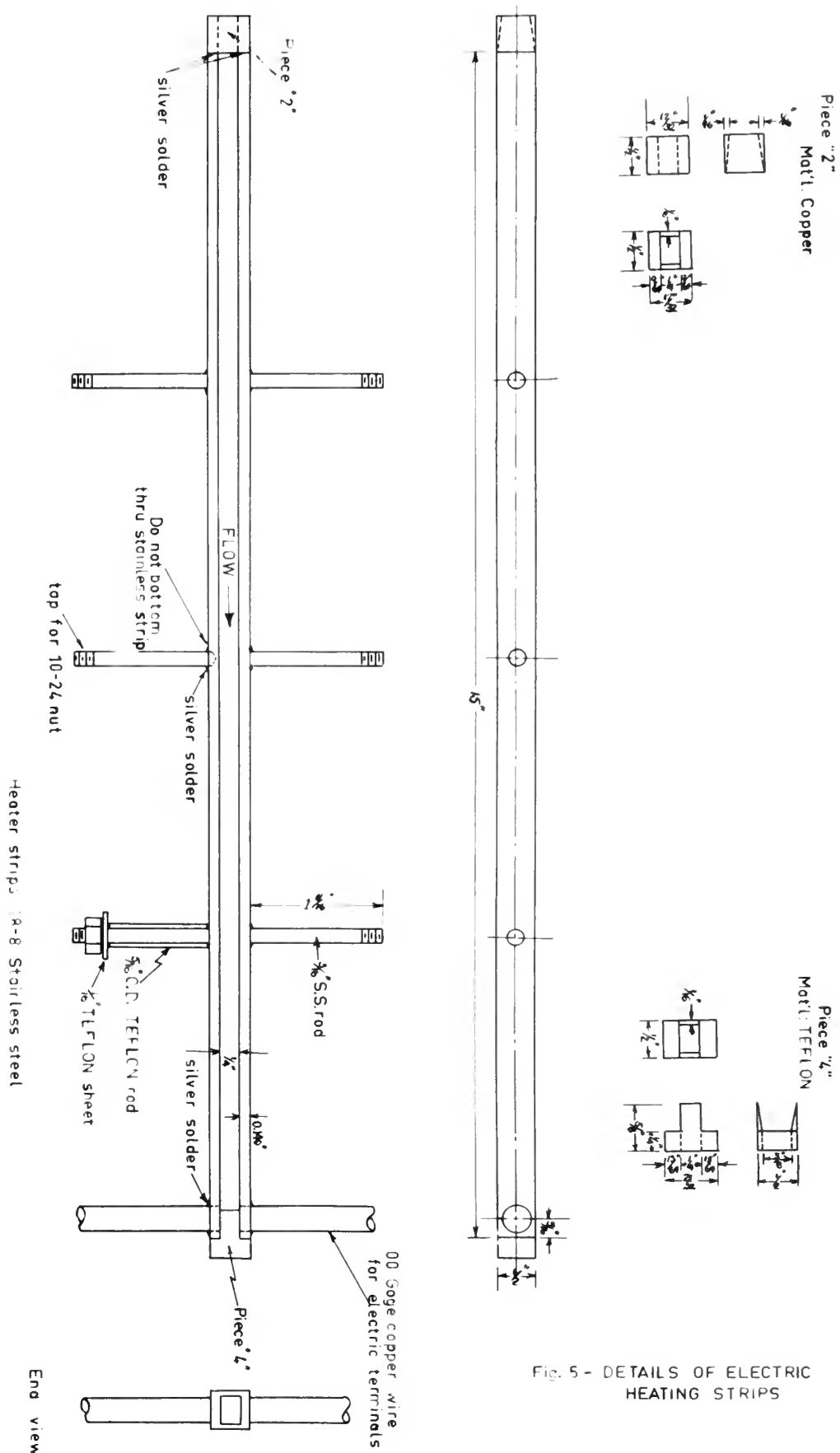
Fig 4 - CENTER SECTION

Duront Teflon plastic. The heater strips were electrically connected in series by a copper bus or connection piece located at the water inlet end of the heater strips (piece "2", Fig. 5). This electrical arrangement was chosen because of the generator characteristics used to provide the electrical power. The power for the heating strips came from a motor-generator set (Motor manufacturer, L.J. Land and Co., 220 volts, 60 cycle, 3 phase, 65 amps, 1150 rpm; generator manufacturer, General Electric Corp., model 53A532, 15 volts, 1000 amps).

The distilled water was degassed by boiling in a stainless steel drum heated by a submerged steam coil using 30 pounds saturated steam. Water was transferred to and from this drum, which also served as a system reservoir, by the Westinghouse pump.

Difficulty was experienced with very small rust particles, apparently from the steel jacketed preheaters, during early runs. A Fulflo Filter BK 10 3/4 Commercial Filter, Corporation, Melrose, Mass., was installed at the 30n pump discharge. This cleared the water satisfactorily.

Originally the test section was in a horizontal position to facilitate the photography. At low flow rates, one to two feet per second in the test section, nucleate boiling bubbles from the lower plate would rise and coalesce with the upper plate bubbles. It was feared that this might cause premature burnout on the upper plate,



so the test section was mounted in a vertical position.

Fig. 5 "Details of Electric Heating Strips" shows the strips as used for the data runs. The first design did not have the six $3/16$ inch stainless steel rod supports for the heating strips, but only two small, $5/32$ inch, diameter, short, $1/4$ inch, stainless steel studs which fastened to a $5/16$ inch TEFLON dowel which in turn was tightened by a nut bearing against the outside of the main body of the test section frame. The small studs located at the midpoint of the strips proved inadequate to prevent compressive buckling of the heated strips during preliminary runs. The larger studs improved the situation, but did not eliminate the bowing of the strips completely. The silver solder on the backs of the strips and the thermal capacity of the larger studs undoubtedly caused variations in the electrical current density and the uniformity of the heat generation, but there was no apparent effect on the bubble boundary layer at the stud locations.

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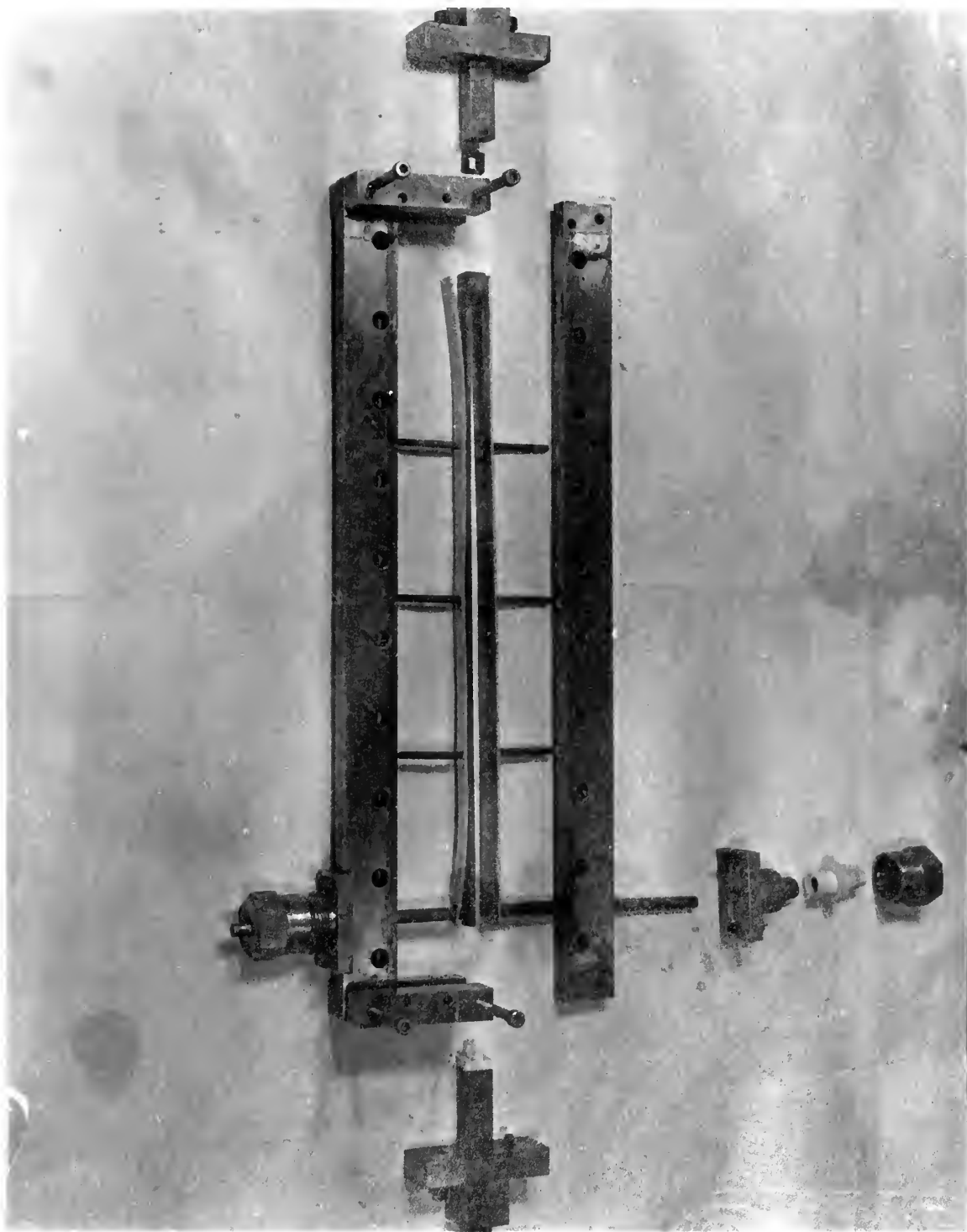


Fig.6 - Photograph of test section
(disassembled)

EXPERIMENTAL PROCEDURE

The distilled water used in the loop was taken from the degassifier where it had been boiled for one hour before each run. The electrical generator loading and the water flow velocity were set while the electrical preheaters were adjusted to maintain the desired water temperature at the test section inlet.

The voltage was measured across the test section electrical terminals with a Weston D.C. voltmeter, model 45, serial 2849, scale 0-1.5, 15, 150 volts. The ammeter on the motor generator control board gave the current readings. The boiling in the test section would cause appreciable increases in the system pressure. This necessitated readjustments in the flow as the pump characteristics were pressure sensitive. Conditions were allowed to stabilize by observing the test section outlet pressure. This pressure generally steadied within one minute. Photographs were taken with a Graphic View 4 inch x 5 inch still camera having Rapax lens, Wollensak Co., using Panatomic X film. Camera settings used were 1/25 sec and f 22. The test section was backlighted with a microflash light, type 1530-A, General Radio Co., Cambridge, Mass. The light was insufficient to light the entire test section at once, so each photograph covered a length of about eight inches. A typical sequence of photographs

is appended as A. 8. 7 and 9. All of the photographs
and negatives are in the possession of Prof. J.A. Clark.
Time was not available for the intended motion picture
study.

Fig.7- v 1 ft/sec
Q/A 83,000 Btu/hrft²



Fig. 8 v 1 ft/sec
Q/A 166,000 Btu/hr ft²



Fig. 9 - v 1 ft/sec
Q/A 250,000 Btu/hr ft²



An attempt will now be made to correlate the experimental conditions in the channel flow with the free surface flow velocity and fluid properties in the channel flow. The bubble boundary layers and the boundary layers of the two successful runs it is believed that the initial condition was in establishing or defining the initial location of the junction. Before the vapor bubbles grow to a size which is about half of the channel width, the bubble is disturbing the boundary layer of the opposite strip. With bubbles of this size, the photographs show that the flow is not symmetrical. A bubble deflects the flow toward the opposite strip and seems to wipe off the bubbles or reduce the boundary layer thickness there.

The quantity h_2 is the calculated bulk enthalpy at the point of intersection of the bubble boundary layers and is equal to the inlet enthalpy h_1 plus the energy added per pound by the heater strips between the inlet and the point

$$h_2 = h_1 + 2 \left(\frac{Q}{A} \right) \frac{A_x}{\omega}$$

where Q is the rate of heat transfer between the point 2 and the heater strips, A_x is the area of the heater strips, and ω is the mass flow rate. The experimental conditions for the various runs are given on pages 25, 26, and 27. The following table gives the values for the various parameters:

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| Picture | | Picture | |
|---------|-------|---------|-------|
| 7 | -.062 | 14 | -.031 |
| 8 | -.064 | 15 | -.034 |
| 9 | -.027 | 16 | -.035 |
| 10 | -.030 | 17 | -.040 |
| 11 | -.053 | 18 | -.056 |
| 12 | -.043 | 19 | -.039 |
| 13 | -.031 | 20 | -.048 |

The quantities h_f , the saturated liquid enthalpy, and h_{fg} , latent heat of evaporation correspond to the pressure measured at the test section outlet. No hydrostatic correction was made. It is significant that all of the points selected showed a negative "quality" or a bulk enthalpy less than the saturated enthalpy at the point where the vapor appears to be blocking the channel.

It must be remembered, however, that the bubbles are actually three dimensional rather than two as is implied here when the point of intersection is assumed. The actual "quality" is undoubtedly less than the value calculated since all the energy generated in the strips was assumed to be transferred to the fluid. There were certainly heat losses through the back of the heating strips both by conduction and by boiling of water which leaked on to the back of the strip. No theoretical calculations were made to estimate the magnitude of this loss nor was a heat balance attempted

on the section because of inadequate instrumentation. It is believed that the losses are less than 5%, actually.

Several "exploratory" runs were made in an effort to achieve a higher quality at the test section outlet. No photographs were taken. With $Q/A = 455,000 \text{ btu/hr ft}^2$, $v = 1 \text{ ft/sec}$, $t_1 = 170^\circ$ and $p = 45 \text{ psia}$, the calculated quality at outlet was about - 1.4%. The lower two thirds of the channel appeared to be almost all water.

$Q/A = 450,000 \text{ btu/hr ft}^2$, $v = 0.8 \text{ ft/sec}$, $t_1 = 164^\circ$ and $p = 53 \text{ psia}$ gave a pulsating flow with slugs of vapor surging up the channel. The calculated outlet quality was - 4.7%. The highest quality achieved was - 14.4% with $Q/A = 440,000 \text{ btu/hr ft}^2$, $v = 0.5 \text{ ft/sec}$, $t_1 = 175^\circ$ and $p = 60 \text{ psia}$. With these conditions the upper two thirds of the test section was mostly vapor with violent boiling in the bottom third.

Plots were made of δ , the thickness or height of the bubble boundary layer, against a parameter H , which expressed the subcooling of the bulk liquid at the location where δ was measured. H is the same negative "quality" or subcooling spoken of previously.

$$H \equiv \frac{h_s - h_f}{h_{fg}}$$

where

$$h_s = h_i + 2 \left(\frac{Q}{A} \right) \frac{A_s}{\omega}$$

$$\frac{m - \frac{1}{2}m}{m} = \frac{1}{2}$$

$$\frac{m}{m} \left(\frac{1}{2} \right) = \frac{1}{2}$$

and h_g is the calculated enthalpy at the point where δ was measured. The value of H was also calculated ignoring all heat losses. As H is a calculated quantity, the experimental uncertainty is of interest. With the following experimental variations:

flow velocity ± 0.1 ft/sec for $v = 1$ ft/sec

pressure ± 0.5 psia

inlet temperature $\pm 0.5^\circ\text{F}$

generator current ± 5.0 amps

the resulting uncertainty in H can be estimated. Taking run #29, which is Fig. 8, as an example where $\delta = .083$ inches at a distance $x = 9.35$ inches from the beginning of the heated strip.

$$Q = 8.3 \text{ volts} \times 600 \pm 5 \text{ amps} = 4.72 \pm 0.4 \text{ Btu/sec}$$

$$w = .11 \pm .01 \text{ lb/sec}$$

$$h_g = h_i + Q \cdot \frac{1}{w} \left(\frac{x}{L} \right) \quad L = 14.7'' \text{ length of heated strip}$$

$$\text{with } t_i = 200^\circ\text{F} \pm 0.5^\circ\text{F}, h_i = 168.0 \pm 0.5 \text{ Btu/lb}$$

$$\text{since } p = 41 \pm 0.5 \text{ psia}$$

$$h_f = 237.5 \pm 0.7 \text{ Btu/lb}$$

$$h_{fg} = 932.6 \pm 0.5 \text{ Btu/lb}$$

$$H = \frac{h_g - h_f}{h_{fg}}$$

$$H = \frac{(195.3 \pm 3.3) - (237.5 \pm 0.7)}{932.6 \pm 0.5}$$

$$H = 0.045 \pm .003$$

This shows an uncertainty of about 6% in H . The largest variations were in the water velocity and the generator current measurements, consequently the scatter was appreciably greater for the low flow and low power runs. This is quite possibly the explanation for the seeming inconsistencies shown on Fig. 10 where $Q/A \approx 33,000$ Btu/hr ft² and the 3 ft/sec is to the right of the 2 ft/sec run.

The plots of δ vs h show that the growth of the bubble boundary layer is as would be expected. It is less for the greater subcooling and higher velocities while greater for the higher heat flux densities. These variations are given quantitatively by the graphs. Since the general shape of the various curves is similar, it was thought that a correlation for the nucleation points (i.e.

$\delta = 0$) might be found. As the pressure was different for the various runs, a pressure parameter for nucleation was sought. Using the liquid superheat at incipient nucleation, a term was added to the "subcooling" parameter H used previously. If

$$(t_w^* - t_f) = f(p)$$

where t_w^* is the wall temperature at the point of nucleation and t_f is the bulk fluid temperature.

$$h_w^* - h_g = f(p)$$

$$(7.0 \pm 2.7\text{e}) - (6.6 \pm 2.3\text{e}) = 1.4$$

20 * 2.56P

200. 250.0 = H

[illegible]

If p is constant then h_f and h_{fg} are constant,

$$\frac{(h_w - h_f)^* + (h_f - h_g)}{h_{fg}} = \frac{h_w^* - h_g^*}{h_{fg}}$$

$$M \equiv \left(\frac{h_w - h_f}{h_{fg}} \right) - H \quad \text{where} \quad H = \frac{h_g^* - h_f}{h_{fg}}$$

Values for $t_w^* - t_f$ as a function of pressure were taken from Figure IV-C-2 "Maximum Experimental and Theoretical Degree of Liquid Superheat" from ref. (3).

The experimental superheat curve for the stainless steel - water system was used. The pressure nucleation correction was applied to smoothed curves of δ vs M . The resulting correlation is shown in Fig. 21. While it is true that this resulted in a closer grouping of the data, such a high value of superheat ($\sim 150^\circ\text{F}$) obtained in an experiment where the water was very clean, unagitated and static is unlikely in a moving fluid being heated. It is felt that a superheat of about thirty degrees would be more reasonable. Any such lower value of superheat would tend to scatter the curves more. It is apparent that a generalized correlation is yet to be gained.

10. The following is a list of the names of the persons who have been

$$\frac{\frac{1}{2}N - \frac{1}{2}N}{\frac{1}{2}N} = \frac{(2N - 1) + (2N - 1)}{\frac{1}{2}N}$$

$$\frac{2N - 1}{\frac{1}{2}N} = 4 \quad \text{where} \quad 4 - \left(\frac{2N - 1}{\frac{1}{2}N} \right) = 1$$

11. The following is a list of the names of the persons who have been

12. The following is a list of the names of the persons who have been

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25. The following is a list of the names of the persons who have been

LIST OF SYMBOLS

| | | |
|--------------|---|---------------------------|
| A_{δ} | area of heater strip from inlet to point where δ was measured | (sq. in.) |
| A_x | area of heater strip from inlet to point where $\delta = 1/2 y$ | (sq. in.) |
| | height of bubble boundary layer | (in.) |
| h_{δ} | fluid enthalpy at point where δ is measured | (Btu/lb) |
| h_f | enthalpy of liquid | (Btu/lb) |
| h_{fg} | latent heat of evaporation | (Btu/lb) |
| h_1 | fluid enthalpy at test section inlet | (Btu/lb) |
| h_x | fluid enthalpy at point x | (Btu/lb) |
| H | "subcooling" parameter $= \frac{h_{\delta} - h_f}{h_{fg}}$ | |
| L | length of heated strip | (in.) |
| M | "nucleation - subcooling" parameter $= \frac{(h_w - h_f^*) - (h_{\delta}^* - h_f)}{h_{fg}}$ | |
| p | test section outlet pressure | (psi) |
| q/A | heat flux density | (Btu/hr ft ²) |
| t_w | temperature of heated wall | (°F) |
| t_f | temperature of fluid | (°F) |
| v | flow velocity | (ft/sec) |
| w | mass flow rate | (lb/sec) |
| x | distance from inlet where δ is measured | (in.) |
| y | spacing between heater strips | (in.) |
| * | indicates conditions at bubble nucleation | |

$$\frac{(x^2 - 2x) - (x^2 - 2x)}{x^2} =$$

$$\frac{x^2 - 2x}{x^2} =$$

3

Experimental and Calculated Data on the Hubble Boundary Layer

| Elect. Volts | amps | ω/λ | v ft/sec | t_1 OF | P psia | δ in. | x in. | -H |
|--------------|-------|------------------|---------------|-------------|-------------|--|---|--|
| #1 4.5 | 330 | 43,000 | 1 | 180 | 15 | .00 .04 .081 .081 | 2.11 7.85 9.27 10.96 | .029 .026 .025 .022 |
| #2 5.9 | 430 | 83,000 | 1 | 180 | 17 | .00 .016 .032 .089 .113 | 4.20 5.78 8.30 9.11 10.71 | .035 .032 .028 .027 .025 |
| #3 7.8 | 505 | 147,000 | 1 | 180 | 28 | .00 .04 .050 .072 .113 | 4.75 3.59 0.49 0.15 10.23 | .007 .004 .050 .052 .046 |
| #5 8.4 | 505 | 166,000 | 2 | 180 | 22 | .00 .024 .032 .004 .072 | 2.75 4.27 5.89 8.05 10.01 | .050 .047 .044 .041 .038 |
| #6 10.3 | 730 | 250,000 | 2 | 180 | 20 | .00 .034 .034 .052 .00 .080 | 2.45 3.01 4.84 7.0 9.15 10.89 | .001 .059 .055 .050 .045 .041 |
| #7 12.5 | 920 | 416,000 | 2 | 180 | 48 | .00 .075 .09 .11 | 1.75 8.10 9.05 10.41 | .100 .075 .070 .066 |
| #8 15.0 | 1,000 | 500,000 | 2 | 180 | 50 | .00 .082 .108 .125 | 1.75 7.75 8.75 9.00 | .114 .082 .078 .070 |
| #9 8.3 | 605 | 100,000 | 3 | 180 | 17 | .00 .092 .10 .125 .083 .117 | 2.87 8.20 9.53 10.87 11.75 12.71 | .038 .033 .031 .030 .029 .028 |
| #10 10.3 | 730 | 250,000 | 3 | 180 | 20 | .00 .043 .078 .080 .104 .12 | 2.75 8.27 9.47 9.71 10.85 12.55 | .046 .038 .030 .030 .034 .031 |
| #11 12.3 | 850 | 333,000 | 2 | 180 | 30 | .00 .117 .109 .107 .117 | 1.87 8.45 9.71 10.02 11.57 | .083 .070 .067 .065 .063 |
| #12 12.3 | 850 | 333,000 | 3 | 180 | 20 | .00 .000 .083 .108 .117 | 4.45 7.00 8.34 9.59 10.33 | .001 .050 .049 .040 .045 |
| #13 12.3 | 850 | 333,000 | 4 | 180 | 20 | .00 .042 .000 .063 .10 | 4.75 7.85 9.0 9.00 10.90 | .040 .038 .036 .036 .034 |
| #14 12.3 | 850 | 333,000 | 5 | 174 | 17 | .00 .041 .000 .060 .066 | 3.0 7.75 8.84 9.75 | .040 .040 .039 .038 |
| #15 12.2 | 855 | 333,000 | 5 | 180 | 19 | .00 .009 .078 .112 .129 | 2.87 8.94 9.99 11.51 13.42 | .047 .037 .035 .034 .031 |

Experimental and Calculated Data on the Subtle Boundary Layer

| Fict. Volts | amps ϵ/λ | v ft/sec | t_1 of | p psia | δ in. | x in. | -h | Fict. Volts | amps ϵ/λ | v ft/sec | t_1 of | p psia | δ in. | x in. | -h | |
|-------------|-------------------------|-------------|-------------|-----------|-----------------|---|---|-------------|-------------------------|-------------|-------------|-----------|-----------------|---|--|--|
| #16 13.5 | 930 | 410,000 | 5 | 180 | 22 | .06 .067 .058 .041 .075 .039 .075 .038 .067 .064 .034 | 3.0 8.0 8.5 5.84 9.82 10.02 11.6 12.0 | #25 5.8 | 435 | 83,000 | 3 | 200 | 20 | .06 .042 .060 .033 .067 .083 .075 .077 .117 .108 .108 | 4.37 0.45 0.87 7.50 8.04 8.71 9.0 9.75 10.42 11.07 12.84 | .020 .027 .025 .025 .025 .025 .024 .024 .024 .023 .023 |
| #17 13.4 | 925 | 410,000 | 4 | 180 | 24 | .06 .042 .03 .017 .083 .092 .033 .03 .013 | 2.37 8.29 5.53 9.03 9.40 9.87 10.29 11.21 11.82 | #26 8.3 | 000 | 100,000 | 4 | 200 | 21 | .06 .05 .033 .067 .108 .075 .108 .10 .06 | 4.12 8.93 9.20 9.90 10.67 11.12 12.04 13.02 14.12 | .032 .027 .027 .027 .020 .020 .024 .024 .024 |
| #18 13.5 | 925 | 410,000 | 3 | 180 | 32 | .06 .084 .108 .025 | 1.87 7.39 8.71 9.28 | #27 8.3 | 000 | 100,000 | 3 | 200 | 23 | .06 .060 .075 .058 .067 .083 .075 .05 .06 | 8.75 7.84 8.33 9.03 9.35 9.94 10.91 11.08 12.95 | .037 .032 .031 .030 .030 .029 .028 .025 .020 |
| #20 14.5 | 990 | 470,000 | 4 | 180 | 29 | .06 .058 .067 .017 .042 .042 .06 | 4.0 8.04 5.75 9.3 10.0 11.3 12.0 | #28 8.3 | 000 | 100,000 | 2 | 200 | 27 | .06 .067 .075 .071 .06 .041 .041 | 5.37 7.95 8.21 8.44 8.17 8.87 | .049 .040 .040 .040 .036 .037 .037 |
| #22 15.7 | 430 | 83,000 | 1 | 200 | 25 | .06 .067 .075 .071 .06 .041 .041 | 4.75 6.0 7.05 7.75 11.0 12.09 13.0 | #29 8.3 | 000 | 100,000 | 1 | 200 | 41 | .06 .054 .075 .058 .063 .063 .045 .042 .042 | 7.70 8.27 8.53 8.75 9.35 9.75 10.35 11.90 | .068 .050 .048 .047 .045 .044 .044 .037 .037 |
| #24 15.7 | 430 | 83,000 | 2 | 200 | 20 | .06 .042 .067 .06 .067 .05 .071 .083 .075 .044 | 7.07 8.44 8.09 8.57 9.37 9.02 9.70 10.28 10.44 10.82 | #30 10.5 | 725 | 450,000 | 2 | 200 | 50 | .06 .067 .084 .10 .06 .06 .047 | 7.93 8.47 8.45 9.41 9.75 10.35 11.90 | .049 .040 .038 .037 .036 .035 .034 .034 |

Calculated Values of the "Nucleation and Subcooling"
Parameter M for smoothed curves of δ

| Fict. | δ | $(t_w - t_f)^*$ | M | Fict. | δ | $(t_w - t_f)^*$ | M |
|-------|----------|-----------------|------|-------|----------|-----------------|-------|
| #2 | 0 | 160 | .200 | #16 | 0 | 150 | .206 |
| | .05 | | .193 | | .05 | | .197 |
| | .10 | | .191 | | .10 | | .194 |
| #3 | 0 | 142 | .215 | #17 | 0 | 147 | .212 |
| | .05 | | .206 | | .05 | | .201 |
| | .10 | | .198 | | .10 | | .197 |
| #6 | 0 | 144 | .197 | #18 | 0 | 136 | .220 |
| | .05 | | .188 | | .05 | | .206 |
| | .10 | | .184 | | .10 | | .200 |
| #7 | 0 | 120 | .229 | #20 | 0 | 140 | .216 |
| | .05 | | .204 | | .05 | | .202 |
| | .10 | | .198 | | .10 | | .198 |
| #8 | 0 | 114 | .235 | #22 | 0 | 145 | .190 |
| | .05 | | .212 | | .05 | | .183 |
| | .10 | | .203 | | .10 | | .178 |
| #9 | 0 | 160 | .203 | #24 | 0 | 154 | .187 |
| | .05 | | .198 | | .05 | | .184 |
| | .10 | | .193 | | .10 | | .182 |
| #10 | 0 | 154 | .222 | #25 | 0 | 154 | .187 |
| | .05 | | .208 | | .05 | | .184 |
| | .10 | | .203 | | .10 | | .184 |
| #11 | 0 | 131 | .223 | #26 | 0 | 152 | .189 |
| | .05 | | .211 | | .05 | | .185 |
| | .10 | | .208 | | .10 | | .183 |
| #12 | 0 | 144 | .212 | #27 | 0 | 148 | .192 |
| | .05 | | .203 | | .05 | | .1855 |
| | .10 | | .198 | | .10 | | .183 |
| #13 | 0 | 154 | .206 | #28 | 0 | 142 | .199 |
| | .05 | | .198 | | .05 | | .191 |
| | .10 | | .194 | | .10 | | .1855 |
| #15 | 0 | 156 | .216 | #29 | 0 | 126 | .203 |
| | .05 | | .208 | | .05 | | .184 |
| | .10 | | .204 | | .10 | | .179 |
| | | | | #30 | 0 | 114 | .214 |
| | | | | | .05 | | .185 |
| | | | | | .10 | | .178 |

GRAPHIC PLOTS OF DATA

The following figures are arranged first for constant heat flux density Q/A with varying flow velocities to show the velocity effect on the growth of the bubble boundary layer for different subcoolings. The data was next cross-plotted at a constant flow velocity to show the effect of changing heat flux density against subcooling.

The calculation of the heat flux density at the velocity surface of the velocity surface layer for the plotted and calculated values of the operating conditions.

Fig. 10 - $q/A = 83,000 \text{ Btu/hr ft}^2$

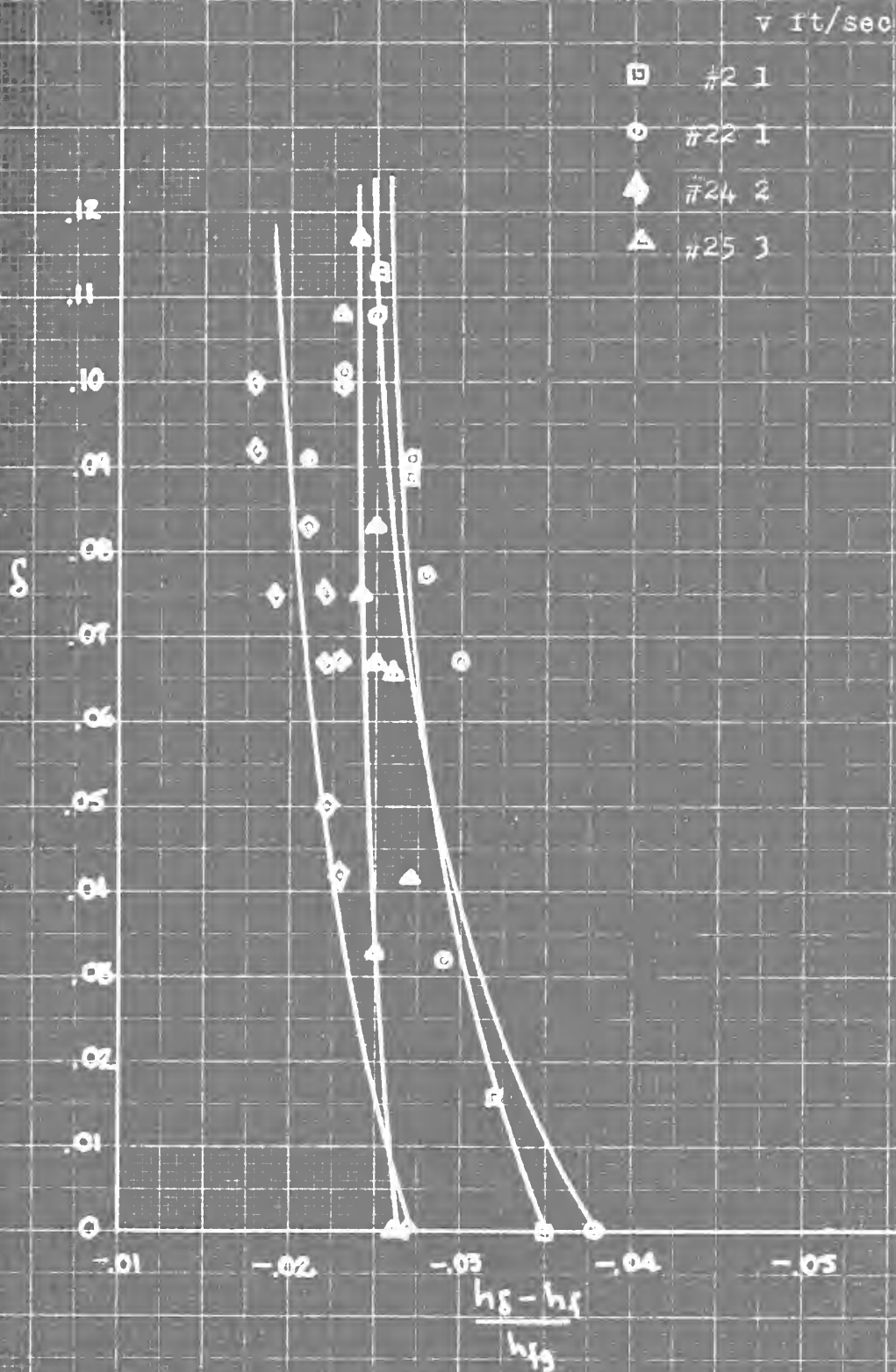


Fig. 11 - $Q/A = 166,000 \text{ Btu/hr ft}^2$

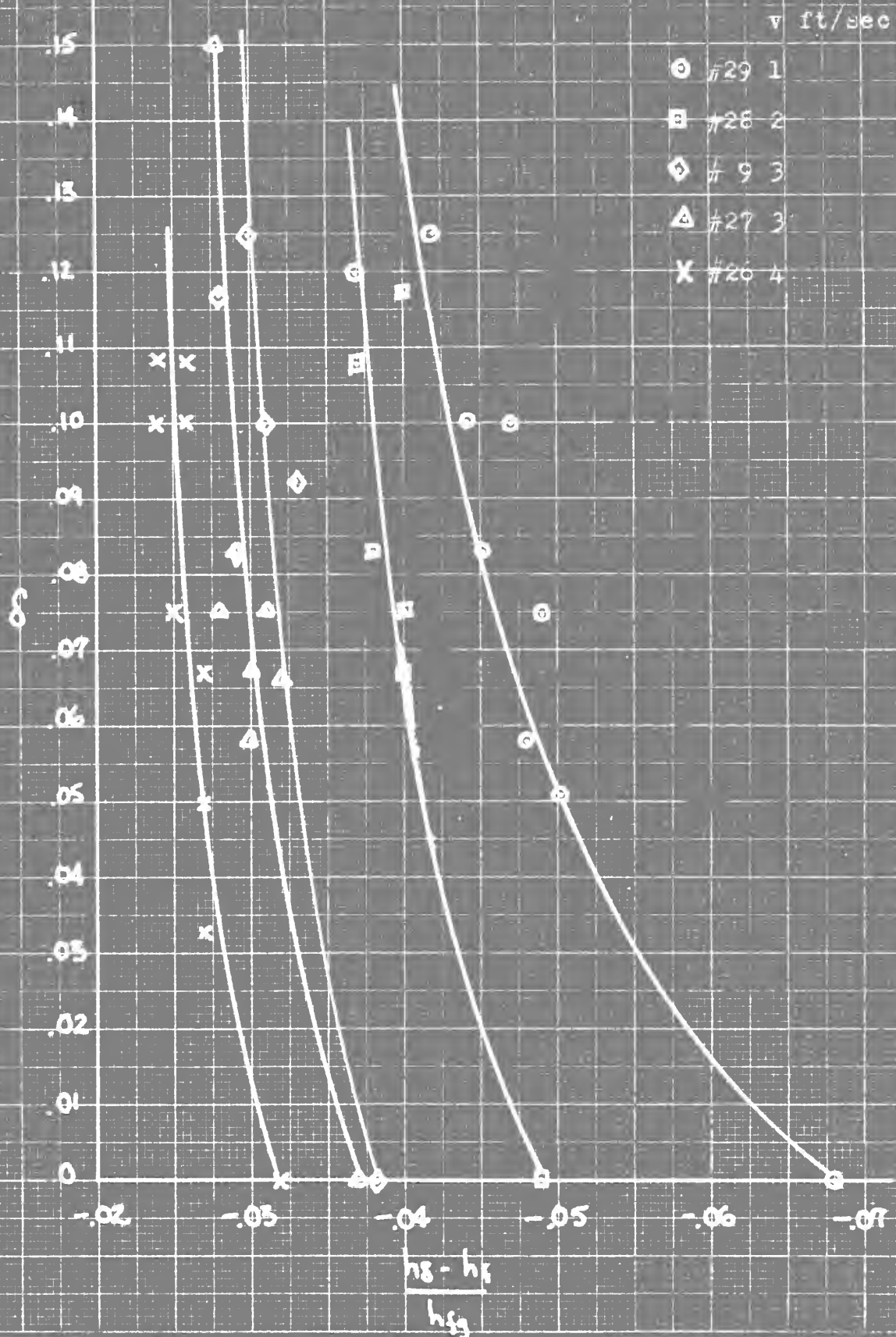


Fig. 12 - $q/a = 250,000$ Btu/hr ft²

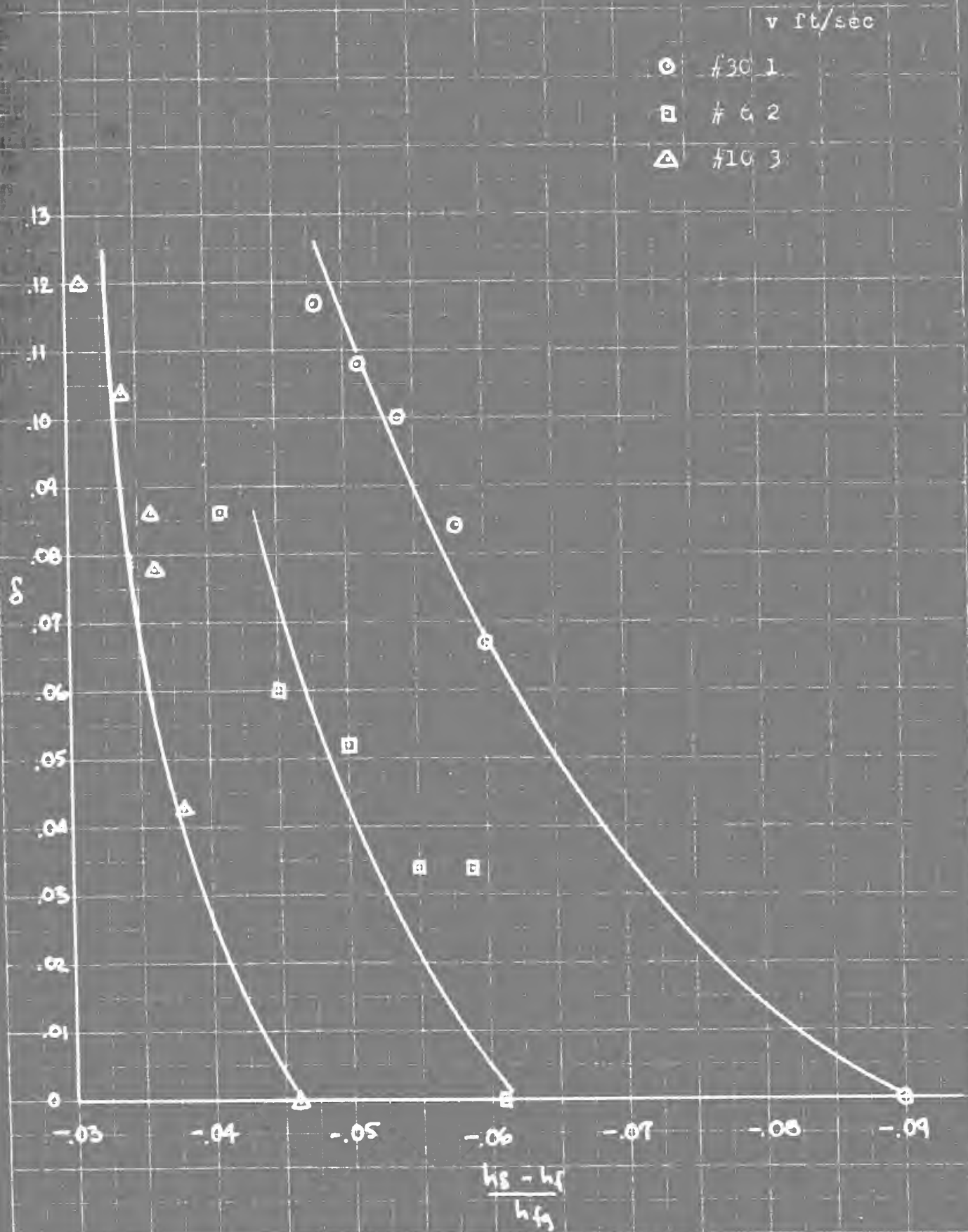


Fig. 13 - $k/A = 333,000 \text{ Btu/hr ft}^2$

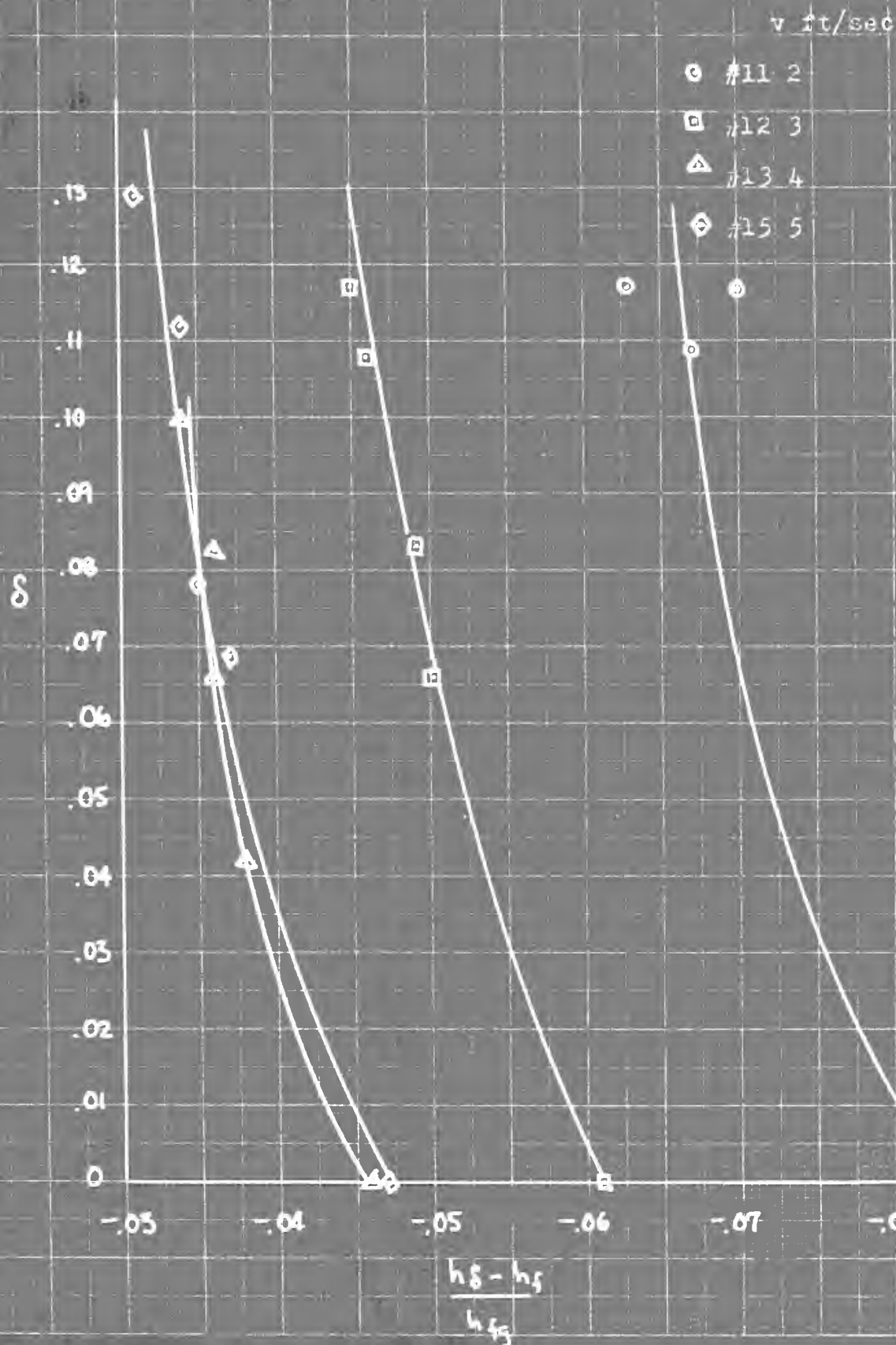


Fig. 15 - $Q/A = 475,000 \text{ Btu/hr ft}^2$

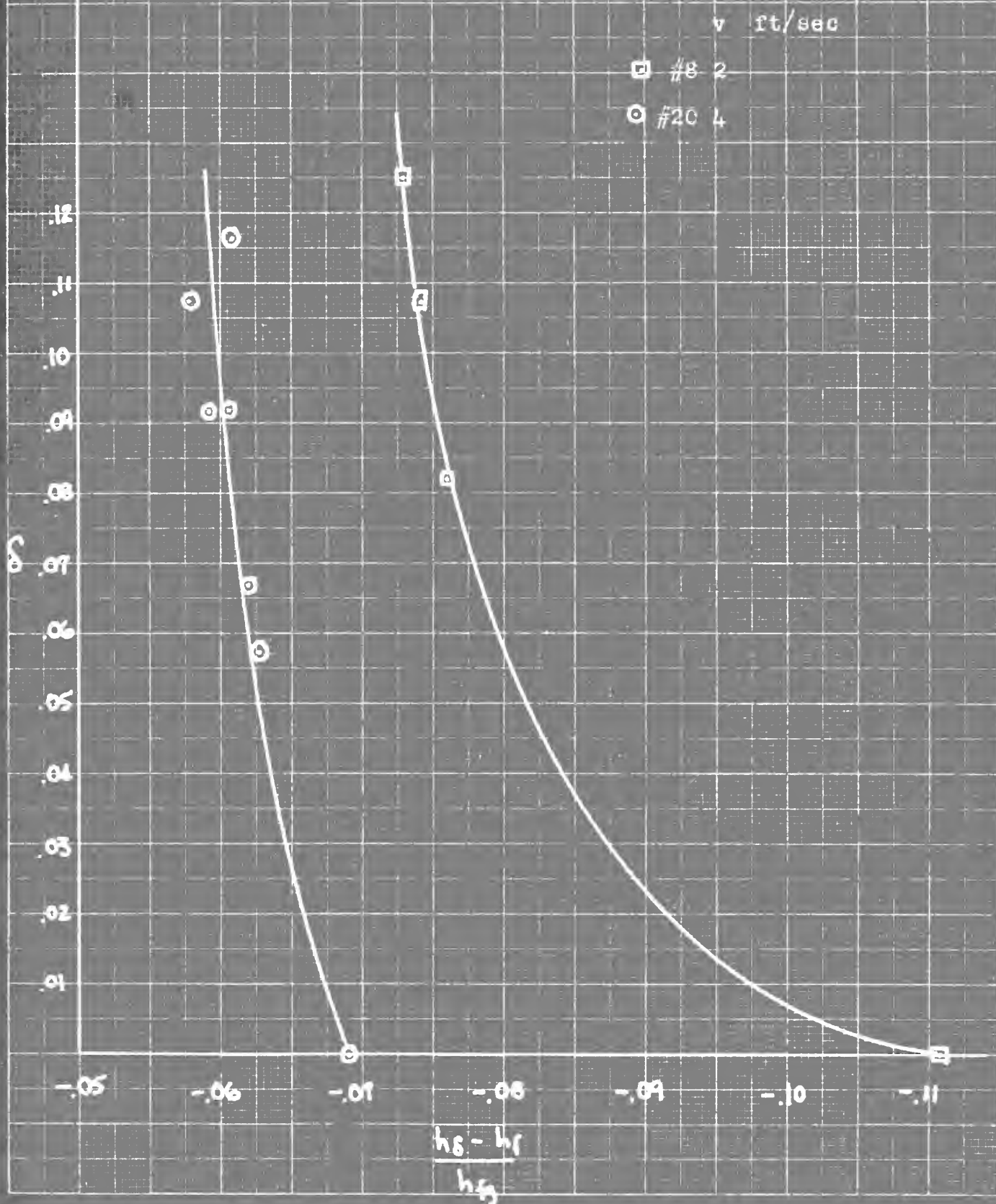


Fig. 18 - $V = 1 \text{ ft/sec.}$

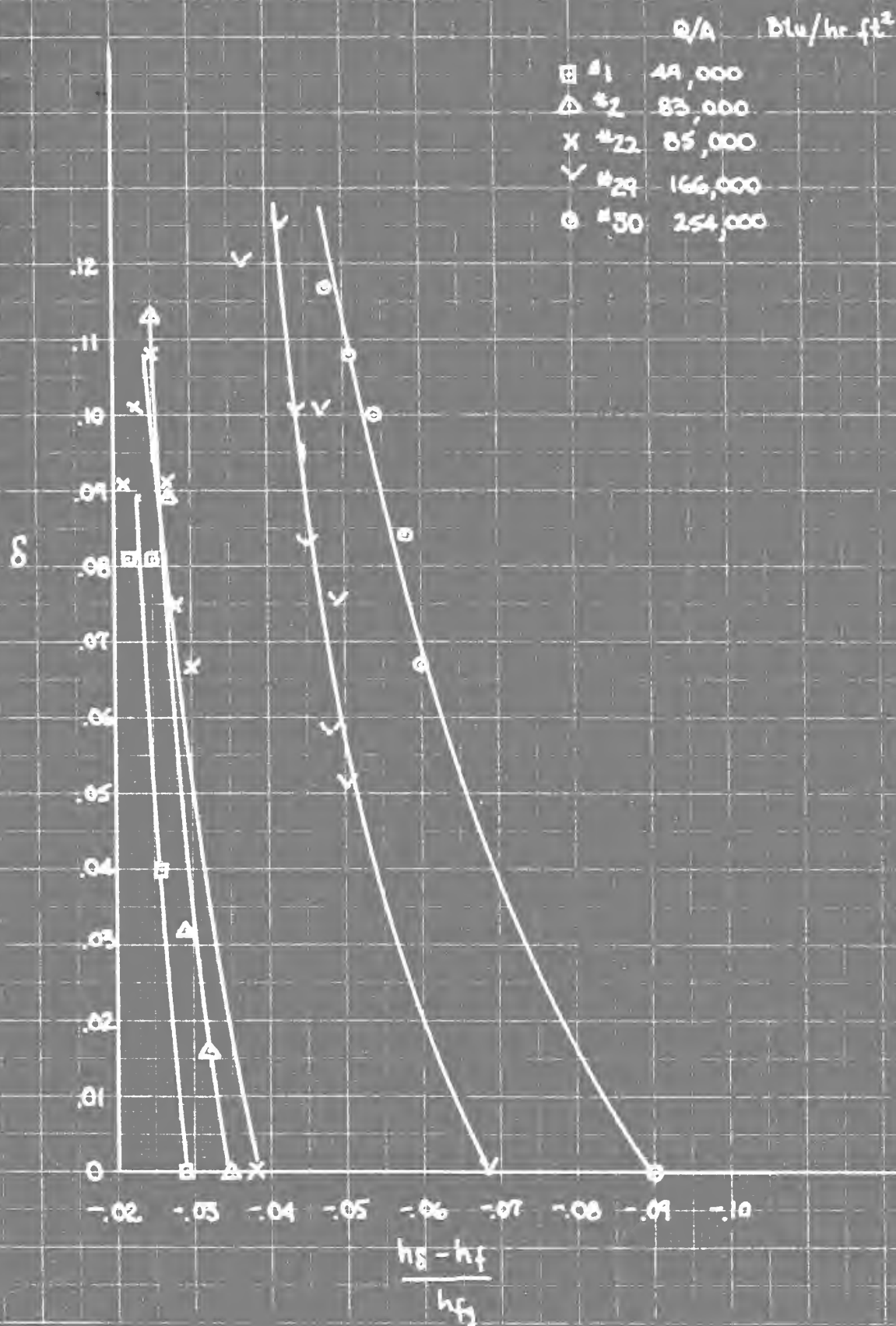


Fig. 17 - $v = 2$ ft/sec

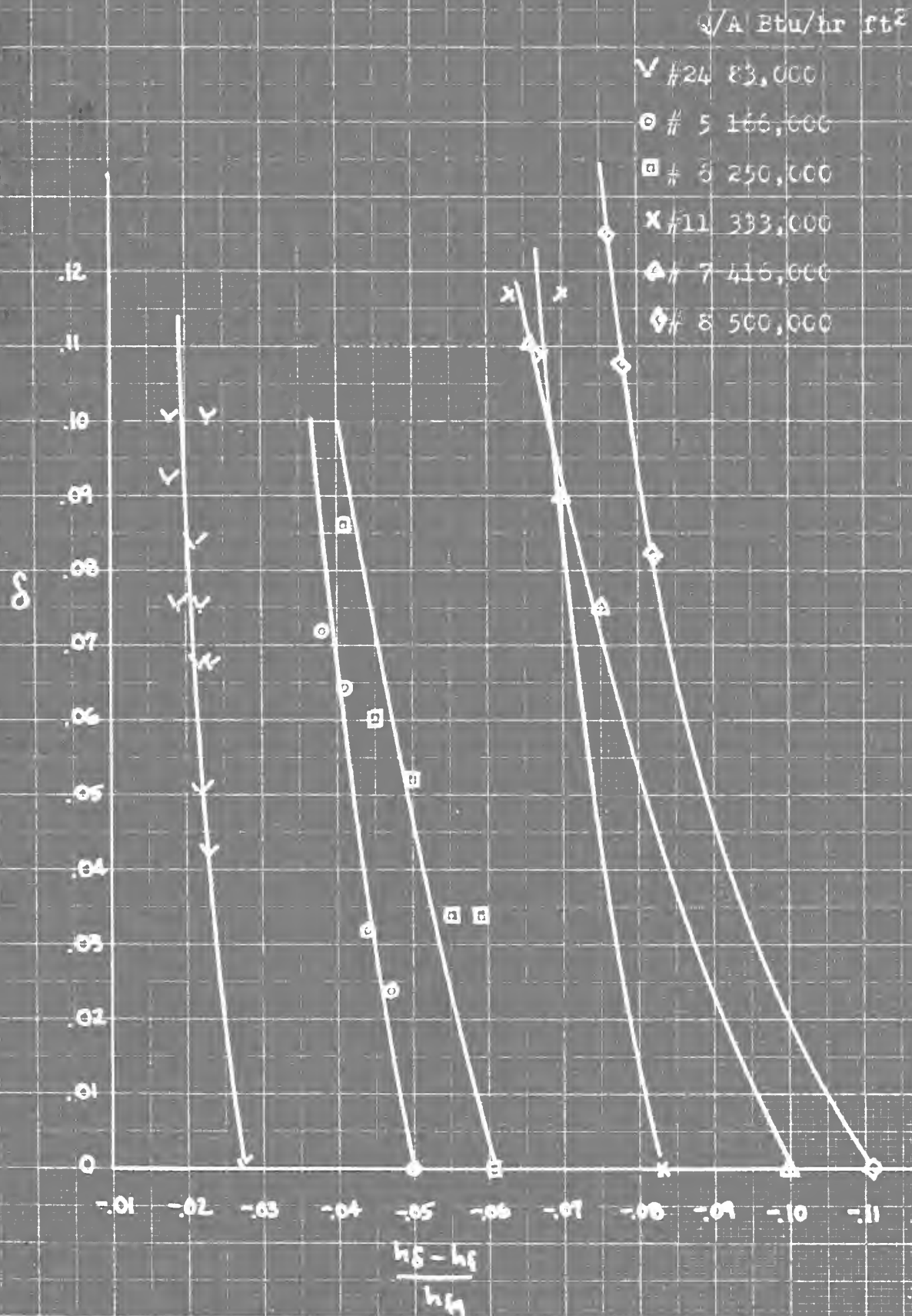


Fig. 18 - $v = 3 \text{ ft/sec}$

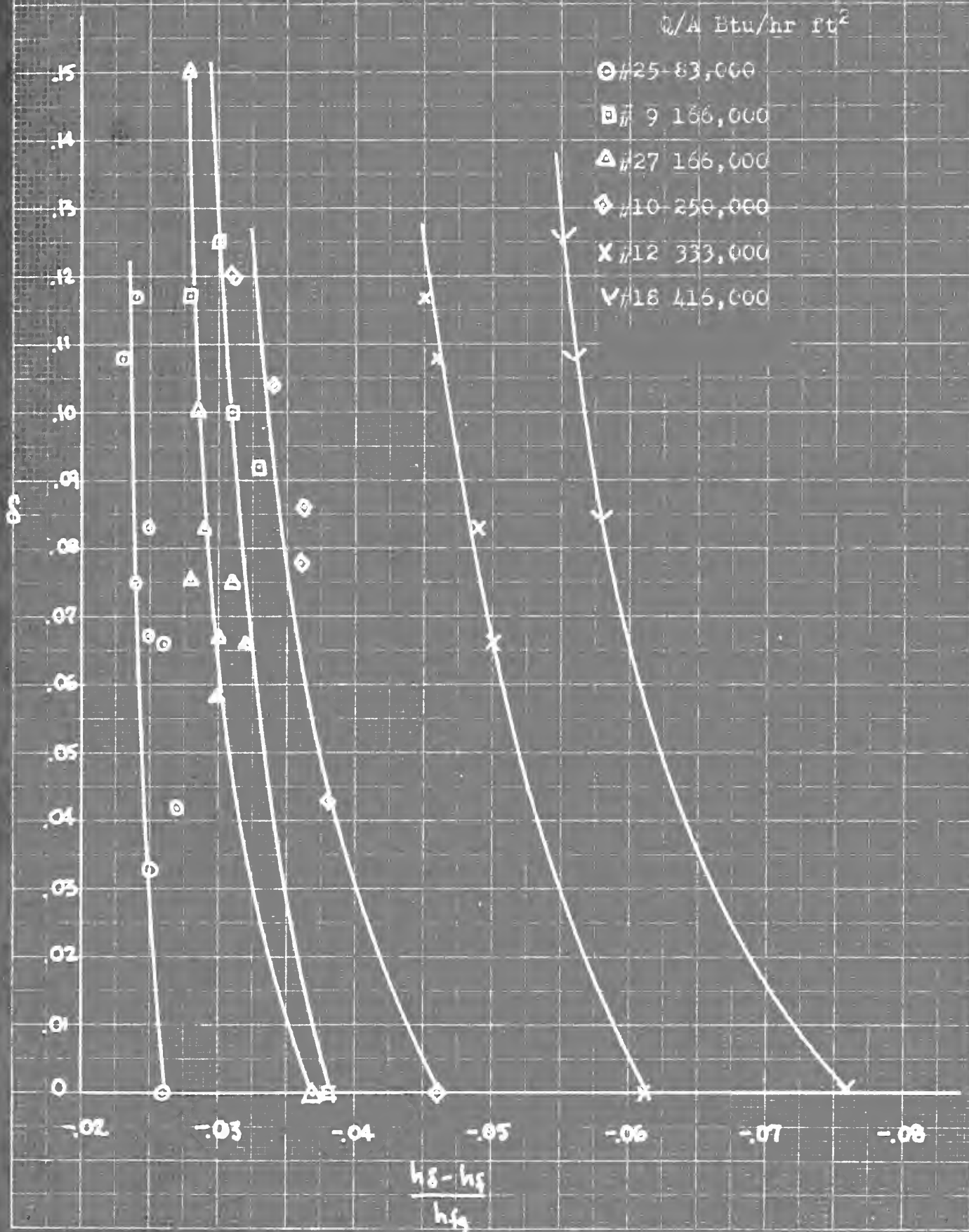


Fig. 19 - $v = 4$ ft/sec

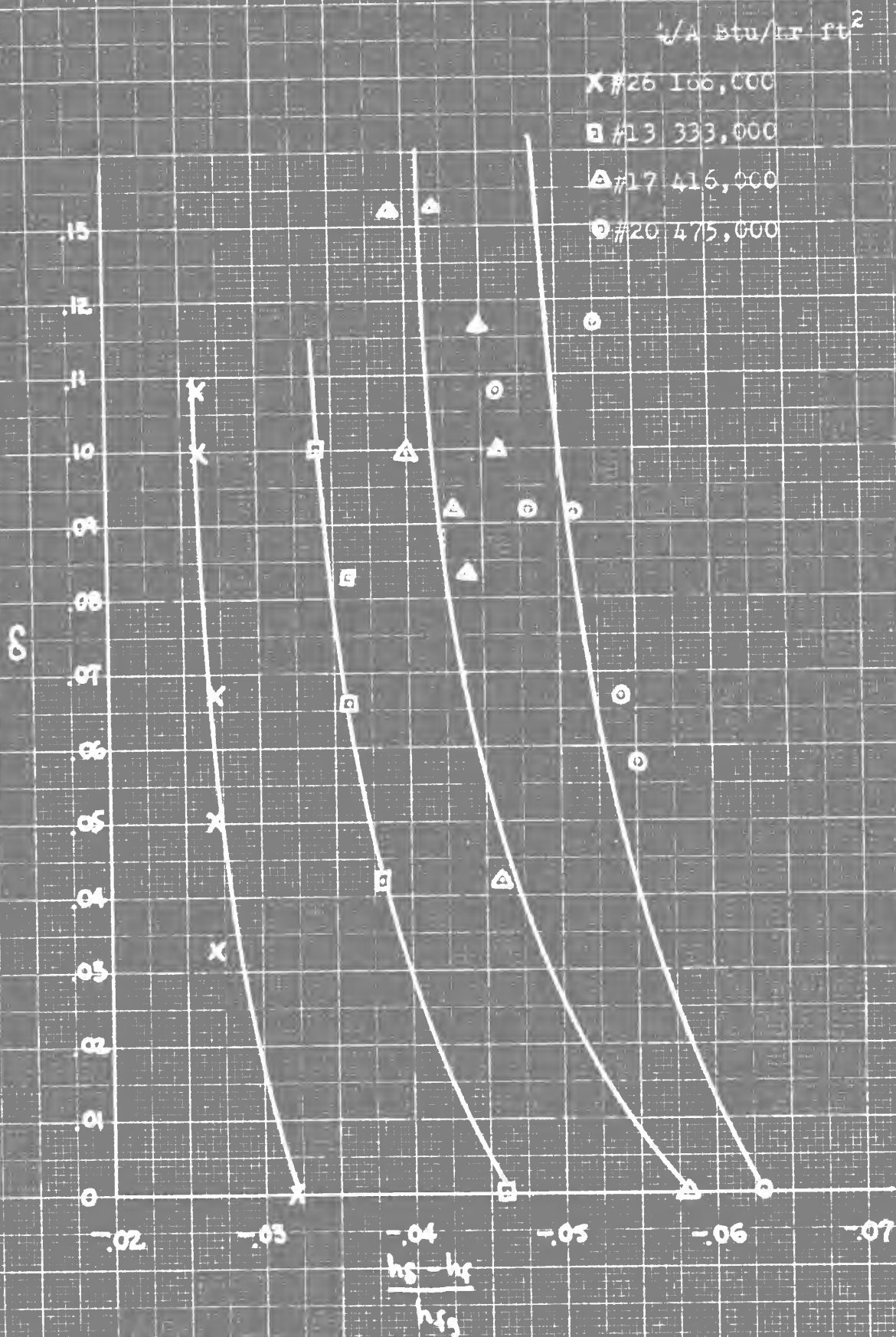


Fig. 20 - $v = 5$ ft/sec

Q/A Btu/lr ft²

◇ #15 333,000

□ #16 416,000

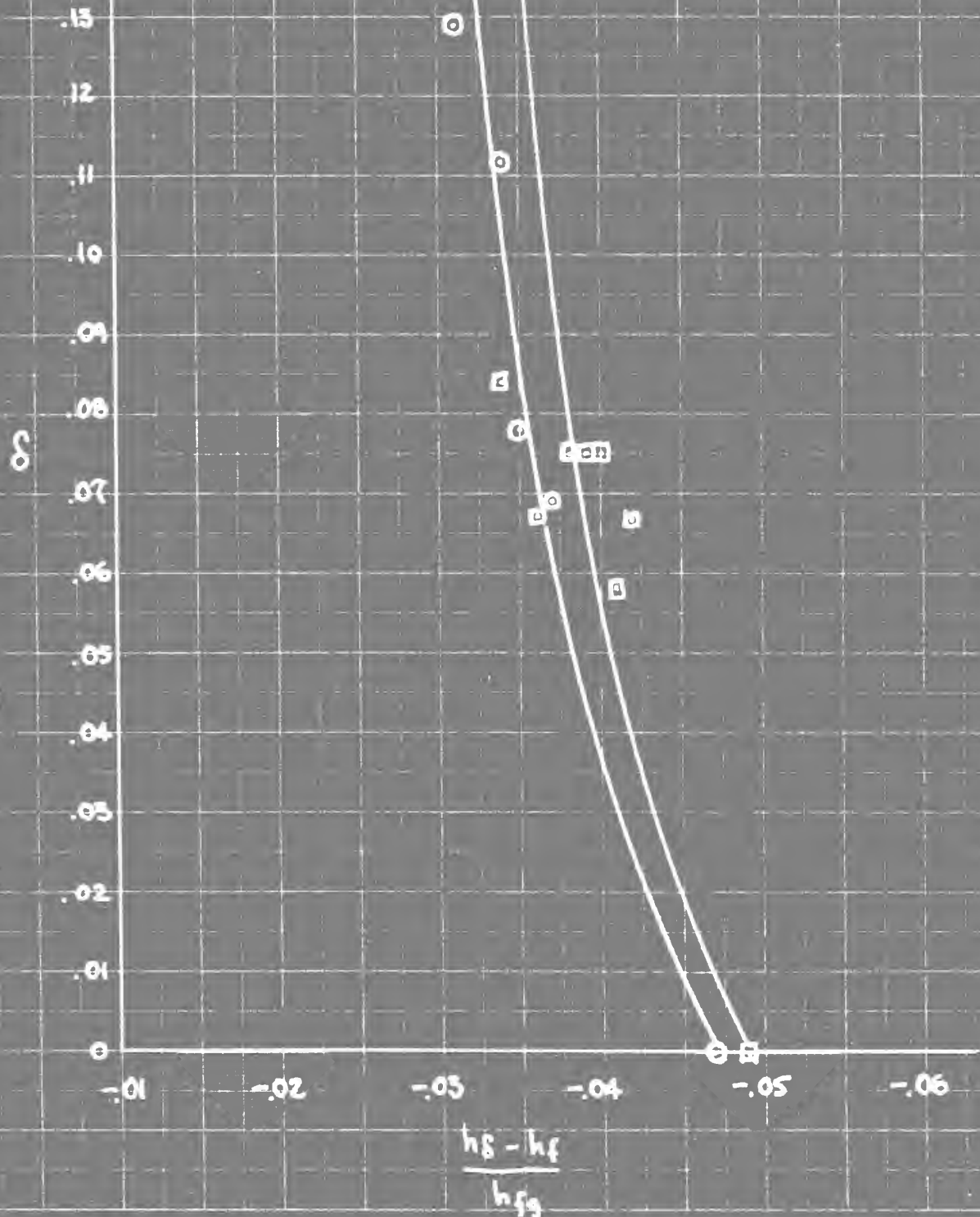
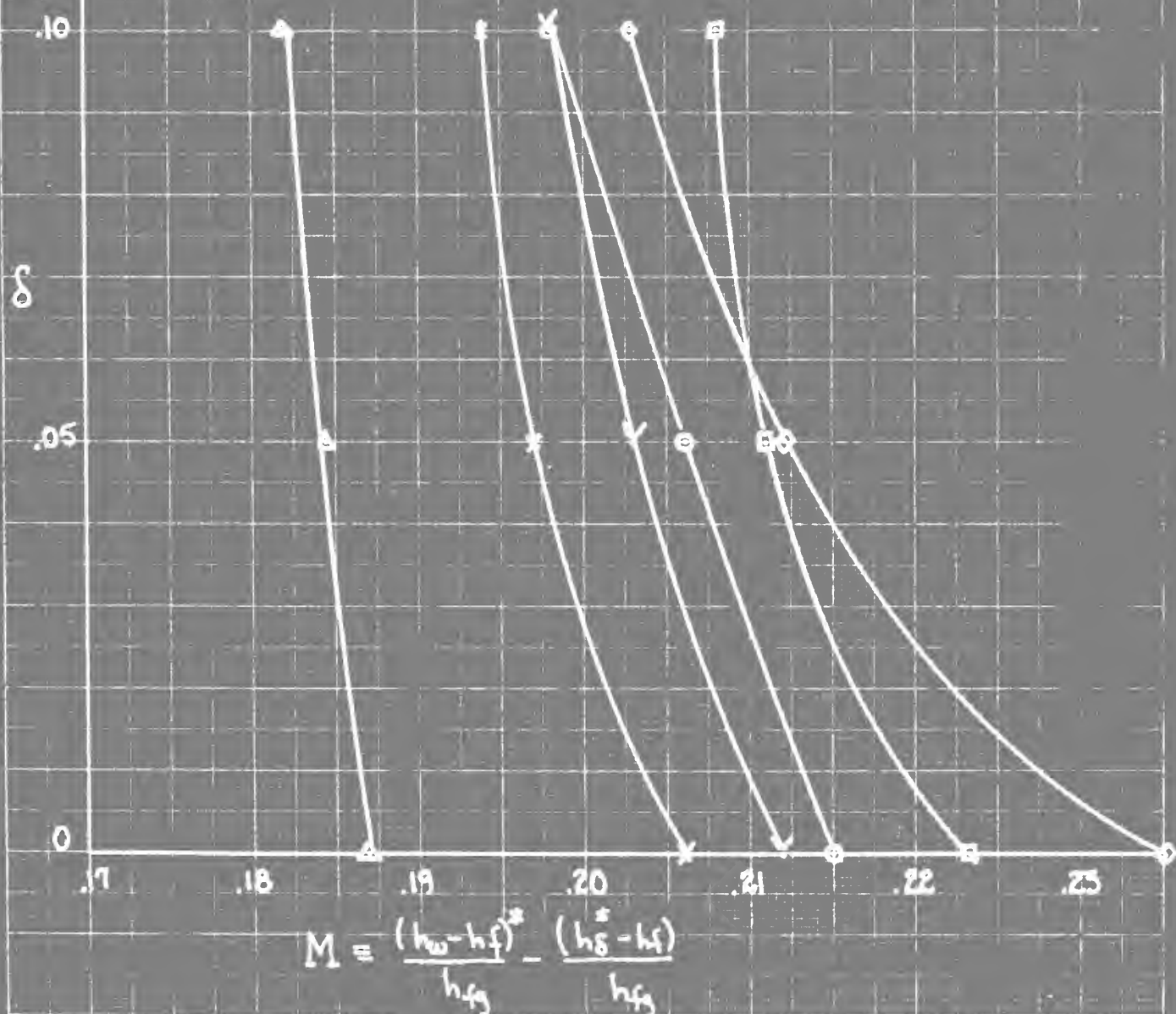


Fig. 21

| | ωA | ν |
|-------|------------|-------|
| ○ #3 | 147,000 | 1 |
| ◇ #8 | 300,000 | 2 |
| □ #11 | 333,000 | 2 |
| △ #24 | 83,000 | 2 |
| × #10 | 410,000 | 5 |
| ▽ #12 | 333,000 | 3 |



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3. "Density Transients in Boiling Liquid Systems" Interim Report 52.17, July 1952, OLA AUCU-2169 Univ. of Cal., Los Angeles, Calif.

1. Introduction

- 1.1. The purpose of this study is to investigate the effects of the proposed system on the performance of the system. The results of the study are presented in the following sections.
- 1.2. The study is organized as follows. Section 2 describes the system architecture. Section 3 describes the experimental setup. Section 4 presents the results of the study. Section 5 discusses the conclusions.
- 1.3. The study is organized as follows. Section 2 describes the system architecture. Section 3 describes the experimental setup. Section 4 presents the results of the study. Section 5 discusses the conclusions.

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